10CS/IS661
USN


## Sixth Semester B.E. Degree Examination, Aug./Sept. 2020 Operations Research

Time: 3 hrs.

Note: Answer any FIVE full questions, selecting atleast TWO questions from each part.

## PART - A

1 a. Explain six phases of Operation Research Study.
(06 Marks)
b. The Sigmaware manufacture company has discontinued the production of a certain unprofitable product which has created considerable excess production capacity. Management is considered devoting this excess capacity to one or more of 3 products. The available capacity on the machine is given below :

| Machine Type | Milling machine | Lathe machine | Grinder |
| :--- | :---: | :---: | :---: |
| Available Time | 400 hrs | 300 hrs | 150 hrs |

The number of machine hours required for each unit of the respective product.

| Machine Type | Product 1 | Product 2 | Product 3 |
| :--- | :---: | :---: | :---: |
| Milling machine | 9 | 4 | 6 |
| Lathe | 5 | 3 | 0 |
| Grinder | 4 | 0 | 1 |

The sales department indicates the sales potential for product 3 exceeds $20 \mathrm{units} /$ week. The unit profit will be $\$ 15, \$ 20, \$ 25$ respectively. The objective is to determine how much of each product the company should produce to maximize the profit. Formulate the LPP.
c. Use Graphical method to solve the problem

Maximize $\mathrm{Z}=2 \mathrm{x}_{1}+\mathrm{x}_{2}$
Subject to $\mathrm{x}_{2} \leq 10$

$$
\begin{gathered}
2 x_{1}+5 x_{2} \leq 60 \\
x_{1}+x_{2} \leq 18
\end{gathered}
$$

(07 Marks)
2 a. Define Slack variable and Surplus variable.
b. Solve the following LPP by Simplex method.

Maximize $Z=5 x_{1}+4 x_{2}$
Subject to $3 x_{1}+5 x_{2} \leq 18$

$$
5 x_{1}+2 x_{2} \leq 12
$$

where $x_{1}, x_{2} \geq 10$.
(10 Marks)
c. Explain the concept of Tie - breaking in Simple method.

3 a. Solve the following LPP by Big - M method.
Maximize $\mathrm{Z}=3 \mathrm{x}-\mathrm{y}$
Subject to $2 x+y \geq 2$

$$
\begin{aligned}
& x+3 y \leq 3 \\
& y \leq 4, x, y \geq 0 .
\end{aligned}
$$

(10 Marks)
b. Solve the following LPP by Two - Phase method

Maximize $Z=15 / 2 x-3 y$
Subject to $3 x-y-z \geq 3$
$x-y+z \geq 2$
where $\mathrm{x}, \mathrm{y} \geq 0$.

4 a. Solve the following LPP by revised simplex method
Maximize $Z=2 x_{1}+x_{2}$
Subject to $3 \mathrm{x}_{1}+4 \mathrm{x}_{2} \leq 6$

$$
6 x_{1}+x_{2} \leq 3
$$

$$
\text { where } x_{1}, x_{2} \geq 0 \text {. }
$$

(12 Marks)
b. Explain the following :
i) The essence of Duality theory
ii) Primal dual relationship.
(08 Marks)

## PART - B

5
a. Use Dual Simple method to solve LPP.

Minimize $Z=2 x_{1}+x_{2}$
Subject to $3 x_{1}+x_{2} \geq 3$

$$
\begin{aligned}
4 x_{1}+3 x_{2} & \geq 6 \\
x_{1}+2 x_{2} & \geq 3, x_{1}, x_{2} \geq 0 .
\end{aligned}
$$

(10 Marks)
b. Briefly discuss about Sensitivity analysis.

6 a. Explain the various steps involved in Hungarian method with example.
(06 Marks)
b. Solve the following assignment problem :

| 12 | 30 | 21 | 15 |
| :--- | :--- | :--- | :--- |
| 18 | 33 | 9 | 22 |
| 44 | 25 | 24 | 21 |
| 23 | 20 | 28 | 14 |

(04 Marks)
c. A company is spending Rs 1000 everyday on transportation of its units from three plants to 4 distribution centers. The supply and demand units with unit cost of transportation are given as

|  | $\mathrm{D}_{1}$ | $\mathrm{D}_{2}$ | $\mathrm{D}_{3}$ |  | Capacity |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{P}_{1}$ | 19 | 30 | 50 | 12 | 7 |
| $\mathrm{P}_{2}$ | 70 | 30 | 40 | 60 | 10 |
| $\mathrm{P}_{3}$ | 40 | 10 | 60 | 20 | 18 |
|  | 5 |  |  | 15 |  |

(10 Marks)

7 a. Define the following with respect to games:
i) Zero - sum game
ii) Pure - strategy
iii) Mixed strategy
iv) Pay off.
(06 Marks)
b. Solve the following game by dominance property:

| 3 | 2 | 4 | 0 |
| :--- | :--- | :--- | :--- |
| 3 | 4 | 2 | 4 |
| 4 | 2 | 4 | 0 |
| 0 | 4 | 0 | 8 |

(08 Marks)
c. Solve the following game by Graphical method :

Player B
Player A

| $\begin{array}{lllll}\mathrm{B}_{1} & \mathrm{~B}_{2} & \mathrm{~B}_{3} & \mathrm{~B}_{4}\end{array}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{A}_{1}$ | 8 | 5 | -7 | 9 |
| $\mathrm{A}_{2}$ | -6 | 6 | 4 | -2 |

(06 Marks)

8 Explain briefly the following :
a. Tabu Search algorithm.
b. Genetic algorithm.
c. Metaheuristics.
d. Simulated Annealing algorithm.

